

## Question Bank

Subject: Quantum Mechanics

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1. What is the Probability amplitude?
2. In which case growth of wave-packet is faster, micro- or macro-particle?
3. With which classical parameter, the Planck's constant can be correlated?
4. What is correspondence principle?
5. What is the value of average energy in Planck's black-body radiation distribution?
6. What is ultraviolet catastrophe?
7. What is de Broglie theorem, and which experiment did verify it in a crystal?
8. What is the limiting value of Planck's constant for classical particle?
9. What is zero-point energy?
10. For a free particle how are its phase velocity and group velocity related?
11. How do the wave functions of fermions and bosons differ?
12. If  $|\psi_1\rangle$  and  $|\psi_2\rangle$  be the wave functions of a classical bullet passing hole-1 and hole-2 in a Young's double-slit experiment, then what is the probability of locating the particle at a point on the screen?
13. What will happen to an electron in the ground-state of a hydrogen atom, if it is radiated by light of energy of 9 eV?
14. How is uncertainty in an operator related to its expectation value?
15. What is completeness theorem?
16. What is projection operator?
17. What is a good quantum number ?
18. How is a quantum oscillator different from a classical oscillator?
19. If  $|\psi\rangle = \frac{1}{2}|\phi_1\rangle + \frac{\sqrt{3}}{2}|\phi_2\rangle$  then the probability of finding  $|\psi\rangle$  in  $|\phi_2\rangle$  is?
20. If  $|a\rangle = \frac{1}{3}\begin{pmatrix} 1 \\ i \\ i \end{pmatrix}$  then find the projection operator  $\hat{P}$ . Show that for Hamiltonian H,  $[\hat{P}, \hat{H}] = 0$

21. If  $L_x$ ,  $L_y$  and  $L_z$  are respectively the  $x$ ,  $y$  and  $z$  components of angular momentum operator  $L$ . The commutator  $[L_x L_y, L_z]$  is equal to?
22. What is the degeneracy of a particle in cubic box having energy  $E_{221}$ ?
23. If the momentum and Hamiltonian operators for a particle are  $\hat{P}$  and  $\hat{H}$  respectively, then write the equation of motion for the particle.
24. What is space quantization?
25. A proton is confined to a cubic box, whose sides have length  $10^{-12} \text{ m}$ . What is the minimum kinetic energy of the proton? The mass of proton is  $1.67 \times 10^{-27} \text{ kg}$  and Planck's constant is  $6.63 \times 10^{-34} \text{ Js}$ .
26. In a region of space, a particle with mass  $m$  and with zero energy has a time-independent wave function  $\psi(x) = Ax e^{-x^2/L^2}$  where  $A$  and  $L$  are constants. Determine the potential energy  $U(x)$  of the particle.
27. An electron is described by the wave function
- $$\psi(x) = \begin{cases} 0, & x < 0 \\ Ce^{-x}(1 - e^{-x}), & x > 0 \end{cases}$$
28. If  $\hat{a}^\dagger$  and  $\hat{a}$  are the creation and annihilation operator respectively, then create  $|n\rangle$  state from an  $|m\rangle$  state,  $n > m$  ?  
Then calculate the average position  $\langle x \rangle$  of the electron.
29. For a spin- $s$  particle, in the eigen basis of  $\hat{S}^2$ ,  $\hat{S}_x$  find the expectation value of  $\langle sm | S_x^2 | sm \rangle$
30. Explain Fermi's golden rule of electronic transition.
31. What is the basic difference between Schrodinger's picture and Heisenberg's picture?
32. For a charged oscillator placed in an electric field,  $E$ , so that
- $$H|\psi\rangle = -\frac{\hbar}{2m} \frac{d^2|\psi\rangle}{dx^2} + \left(\frac{1}{2}m\omega^2 x^2 + qEx\right)|\psi\rangle$$
- and the ground-state energy  $E_n^0 = (n + \frac{1}{2})\hbar\omega$  then find the second order correction to energy.