

# Department of Physics – Unit Test

1. An ideal gas with adiabatic exponent, undergoes a process in which its pressure  $P$  is related to its volume  $V$  by the relation  $P = P_0 - \alpha V$ , where  $P_0$  and  $\alpha$  are positive constants. The volume starts from being very close to zero and increases monotonically to  $P_0/\alpha$ . At what value of the volume during the process does the gas have maximum entropy?

a)  $\frac{P_0}{\alpha(1+\gamma)}$       b)  $\frac{\gamma P_0}{\alpha(1-\gamma)}$       c)  $\frac{\gamma P_0}{\alpha(1-\gamma)}$       d)  $\frac{P_0}{\alpha(1-\gamma)}$

2. The H<sub>2</sub> molecule has a reduced mass  $M=8.35 \times 10^{-28}$  kg and an equilibrium internuclear distance  $R = 0.742 \times 10^{-10}$  m. The rotational energy in terms of the rotational quantum number  $J$  is :

a)  $E_{\text{rot}}(J) = 7J(J-1)\text{meV}$       b)  $E_{\text{rot}}(J) = \frac{5}{2}J(J+1)\text{meV}$   
 b. c)  $E_{\text{rot}}(J) = 7J(J+1)\text{meV}$       d)  $E_{\text{rot}}(J) = \frac{5}{2}J(J-1)\text{meV}$

3. The mean value of random variable  $x$  with probability density  $P(x) = \frac{1}{\sigma\sqrt{\pi}} \exp\left(-\frac{x^2 + \mu x}{2\sigma^2}\right)$

a) 0      b)  $\frac{\mu}{2}$       c)  $-\frac{\mu}{2}$       d)  $\sigma$

4. Self inductance per unit length of a long solenoid of radius  $R$  with  $n$  turns per unit length is:

a)  $\mu_0 \pi R^2 n^2$       b)  $2\mu_0 \pi R^2 n^2$       c)  $\mu_0 \pi R^2 n$       d)  $2\mu_0 \pi R^2 n$

5. How much force does light from a 1.8 W laser exert when it is totally absorbed by an object?

a)  $6.0 \times 10^{-9}$  N      b)  $0.6 \times 10^{-9}$  N      c)  $6.0 \times 10^{-8}$  N      d)  $4.8 \times 10^{-9}$  N

6. A cylindrical shell of mass  $m$  has an outer radius  $b$  and an inner radius  $a$ . The moment of inertia of the shell about the axis of the cylinder is:

a)  $\frac{1}{2}m(b^2 - a^2)$       b)  $\frac{1}{2}m(b^2 + a^2)$       c)  $m(b^2 - a^2)$       d)  $m(b^2 + a^2)$

7. A gas contains particles of type A with fraction 0.8, and particles of type B with fraction 0.2. The probability that among 3 randomly chosen particles at least one is of type A is:

a)0.8      b)0.25      c) 0.33      d) 0.992

8. The half-life of a radioactive nuclear source is 9 days. The fraction of nuclei which are left undecayed after 3 days is:

a)  $7/8$       b)  $1/3$       c)  $5/6$       d)  $1/2^{\frac{1}{3}}$

9. A semicircular piece of paper is folded to make a cone with the center of the semicircle as the apex. The half angle of the resulting cone would be:

a)  $90^{\circ}$       b)  $60^{\circ}$       c)  $30^{\circ}$       d)  $45^{\circ}$

10. Circular fringes are obtained with a Michelson interferometer using 600nm laser light. What minimum displacement of one mirror will make the central fringe from bright to dark?

a) 600nm      b) 300nm      c) 150nm      d)  $120\text{\AA}$

11. In the ground state of hydrogen atom, the most probable distance of the electron from the nucleus, in units of Bohr radius  $a_0$  is:

a)  $\frac{1}{2}$       b) 1      c) 2      d)  $\frac{3}{2}$

12. The adjoint of a differential operator  $d/dx$  acting on a wavefunction  $\psi(x)$  for a quantum mechanical system is :

A)  $d/dx$       b)  $-i\hbar \frac{d}{dx}$       c)  $-d/dx$       d)  $i\hbar \frac{d}{dx}$

13. The number of different Bravais lattices possible in two dimension is:

a)2      b)3      c)5      d)6

14. A transistor in common base configuration has ratio of collector current to emitter current  $\beta$  and ratio of collector to base current  $\alpha$ . Which of the following is true :

a)  $\beta = \frac{\alpha}{\alpha+1}$       b)  $\beta = \frac{\alpha+1}{\alpha}$       c)  $\beta = \frac{\alpha}{\alpha-1}$       d)  $\beta = \frac{\alpha-1}{\alpha}$

15. The central force which results in the orbit  $r = a(1 + \cos\theta)$  for a particle is proportional to :

a)r      b)  $r^2$       c)  $r^{-2}$       d) None of these

16. The maximum relativistic kinetic energy of  $\beta$  particles from a radioactive nucleus is equal to the rest mass energy of the particle. A magnetic field is applied perpendicular to the beam of  $\beta$  particles, which bends it to a circle of radius R. The field is given by :

a)  $3m_0c/eR$       b)  $\sqrt{2}m_0c/eR$       c)  $\sqrt{3}m_0c/eR$       d)  $\sqrt{3}m_0c/2eR$

17. The strength of magnetic field at the center of a regular hexagon with sides of length a

carrying a steady current  $I$  is:

a)  $\mu_0 I / \sqrt{3} \pi a$     b)  $\sqrt{6} \mu_0 I / \pi a$     c)  $3 \mu_0 I / \pi a$     d)  $\sqrt{3} \mu_0 I / \pi a$

18. A point charge  $q$  of mass  $m$  is released from rest at a distance  $d$  from an infinite grounded conducting plane (ignore gravity). How long does it take for the charge to hit the plane ?

a)  $\frac{\sqrt{2} \pi^3 m \epsilon_0 d^3}{q}$     b)  $\frac{\sqrt{2} \pi^3 m \epsilon_0 d}{q}$     c)  $\frac{\sqrt{\pi^3 m \epsilon_0 d^3}}{q}$     d)  $\frac{\sqrt{\pi^3 m \epsilon_0 d}}{q}$

19. Light takes approximately 8 minutes to travel from the Sun to the Earth. Suppose in the frame of the Sun an event occurs at  $t = 0$  at the Sun and another event occurs on Earth at  $t = 1$  minute. The velocity of the inertial frame in which both these events are simultaneous is:

- a)  $c/8$  with the velocity vector pointing from Earth to Sun  
b)  $c/8$  with the velocity vector pointing from Sun to Earth  
c) The events can never be simultaneous - no such frame exists  
d)  $C\sqrt{1 - (1/8)^2}$  with velocity vector pointing from sun to earth

20. A spherical shell of radius  $R$  carries a constant surface charge density  $\omega$  and is rotating about one of its diameters with an angular velocity  $\omega$ . The magnitude of the magnetic moment of the shell is:

a)  $4\pi\sigma\omega R^4$     b)  $4\pi\sigma\omega R^4/3$     c)  $4\pi\sigma\omega R^4/15$     d)  $4\pi\sigma\omega R^4/9$

21. Consider  $N$  non-interacting electrons ( $N \sim N_A$ ) in a box of sides  $L_x, L_y, L_z$ . Assume that the dispersion relation is  $\epsilon(k) = Ck^4$ , where  $C$  is a constant, the ratio of the ground state energy per particle to the Fermi energy is :

a)  $3/7$     b)  $7/3$     c)  $3/5$     d)  $5/7$

22. You receive on average 5 emails per day during a 365 days year. The number of days on average on which you do not receive any emails in that year are:

(a) more than 5    b) more than 2    c) 1    d) none of these

23. An ideal gas has a specific heat ratio  $C_p/C_v$ . Starting at a temperature  $T_1$  the gas undergoes an isothermal compression to increase its density by a factor of two. After this an adiabatic compression increases its pressure by a factor of two. The temperature of the gas at the end of the second process would be:

a)  $\sqrt{2}T_1$     b)  $2T_1$     c)  $T_1/2$     d)  $T_1/\sqrt{2}$

24. A thin air film of thickness  $d$  is formed in a glass medium. For normal incidence, the condition for constructive interference in the reflected beam is (in terms of wavelength  $\lambda$  and integer  $m = 0, 1, 2, \dots$ ):

- a)  $2d = (m - 1/2)\lambda$    b)  $2d = m\lambda$    c)  $2d = (m - 1)\lambda$    d)  $2\lambda = (m - 1/2)d$

25. A bead of mass  $M$  slides along a parabolic wire described by  $z = 2(x^2 + y^2) + 1$ . The wire rotates with angular velocity  $\Omega$  about the  $z$ -axis. At what value of  $\Omega$  does the bead maintain a constant nonzero height under the action of gravity along  $z$  ?

- a)  $\sqrt{g}$    b)  $\sqrt{2g}$    c)  $\sqrt{3g}$    d)  $2\sqrt{g}$

26. If the mean square fluctuations in energy of a system in equilibrium at temperature  $T$  is proportional to  $T^\alpha$ , then the energy of the system is proportional to :

- a)  $T^{\alpha - 2}$    b)  $T^\alpha$    c)  $T^{\alpha / 2}$    d)  $T^{\alpha - 1}$

27. Suppose the spin degrees of freedom of a 2-particle system can be described by a 21-dimensional Hilbert subspace. Which among the following could be the spin of one of the particles ?

- a)  $1/2$    b) 3   c)  $3/2$    d) 2

28. Water is poured at a rate of  $R$  m<sup>3</sup>/hour from the top into a cylindrical vessel of diameter  $D$ . The vessel has a small opening of area  $a$  ( $\sqrt{a} \ll D$ ) at the bottom. What should be the minimum height of the vessel so that water does not overflow ?

- a)  $\infty$    b)  $R^2/2ga^2$    c)  $R^2/2gaD^2$    d)  $8R^2/\pi D^2 g^2$

29. What is the equation of the plane which is tangent to the surface  $4xyz$  at the point  $(1, 2, 2)$  ?

- a)  $x + 2y + 4z = 12$    b)  $4x + 2y + z = 12$    c)  $x + 4y + z = 0$    d)  $2x + y + z = 6$

30. Two equal positive charges of magnitude  $+q$  separated by a distance  $d$  are surrounded by a uniformly charged thin spherical shell of radius  $2d$  bearing a total charge  $-2q$  and centred at the midpoint between the two positive charges. The net electric field at distance  $r$  from the midpoint is?

- a) Zero   b) proportional to  $d$    c) proportional to  $\frac{1}{r^3}$    d) proportional to  $\frac{1}{r^4}$

31. If the Hamiltonian of a classical particle is  $H = (P_x^2 + P_y^2)/2m$ , then  $\langle x^2 + xy + y^2 \rangle$  at temperature  $T$  is equal to:
- a)  $K_B T$                       b)  $(1/2) K_B T$                       c)  $2K_B T$                       d)  $(3/2) K_B T$
32. After the detonation of an atom bomb, the spherical ball of gas was found to be 15 meter radius at a temperature of  $3 \times 10^5$  K. Given the adiabatic expansion coefficient  $\gamma = 5/3$ , what will be the radius of the ball when its temperature reduces to  $3 \times 10^3$  K ?
- a) 156m                      b) 150m                      c) 100m                      d) 50m
33. The electric field  $E = E_0 \sin(\omega t - kz) \hat{x} + 2E_0 \sin(\omega t - kz + \frac{\pi}{2}) \hat{y}$  represents:
- a) a linearly polarized wave                      b) a right hand circularly polarized wave  
c) a left hand circularly polarized wave                      d) an elliptically polarized wave
34. A solid, insulating sphere of radius 1 cm has charge  $10^{-7}$  C distributed uniformly over its volume. It is surrounded concentrically by a conducting thick spherical shell of inner radius 2 cm, outer radius 2.5 cm and is charged with  $-2 \times 10^{-7}$  C. What is the electrostatic potential in Volts on the surface of the sphere?
35. The Fourier transform of the function  $\frac{1}{x^4 + 3x^2 + 2}$  upto the proportionality constant is:
- a)  $\sqrt{2} \exp(-k^2) - \exp(-2k^2)$                       b)  $\sqrt{2} \exp(-k) - \exp(-\sqrt{2}|k|)$   
c)  $\sqrt{2} \exp(-\sqrt{|k|}) - \exp(-\sqrt{2}|k|)$                       c)  $\sqrt{2} \exp(-\sqrt{2}k^2) - \exp(-2k^2)$
36. A cylindrical at temperature  $T = 0$  is separated into two compartments A and B by a free sliding piston. Compartments A and B are filled by Fermi gases made of spin 1/2 and 3/2 particles respectively, If particles in both the compartments have same mass, the ratio of equilibrium density of the gas in compartment A to that of gas in compartment B is:
- a)  $\frac{1}{3^{2/5}}$                       b) 1                      c)  $\frac{1}{2^{2/5}}$                       d)  $\frac{1}{3^{2/3}}$
37. The temperature in a rectangular plate bounded by the lines  $x=0, y=0, x=3$  and  $y=5$ ,  $T = xy^2 - x^2y + 100$  What is the maximum temperature difference between two points on the plate?
38. A sphere of inner radius 1 cm and outer radius 2 cm, centered at origins has a volume

charge density  $\rho_0 = \frac{k}{4\pi r}$ , where  $K$  is a nonzero constant and  $r$  is the radial distance. A point charge of magnitude  $10^{-3}$  C is placed at the origin. For what value of  $K$  in units of C/m<sup>2</sup>, the electric field inside the shell is constant ?

39. Suppose that the number of microstates available to a system of  $N$  particles depends on  $N$  and the combined variable  $UV^2$ , where  $U$  is the internal energy and  $V$  is the volume of the system. The system initially has volume 2m<sup>3</sup> and energy 200 J. It undergoes an isentropic expansion to volume 4m<sup>3</sup>. What is the final pressure of the system in SI units ?
40. Let a particle of mass  $1 \times 10^{-9}$  kg, constrained to have one dimensional motion, be initially at the origin ( $x=0$ m). The particle is in equilibrium with a thermal bath  $K_B T = 10^{-8}$  J. What is  $\langle x^2 \rangle$  of the particle after a time  $t = 5$ s?